

Evaluating Definite Integrals Mr. Kouichek
6.5 Pg 463 (1, 2, 9, 10, 15, 29)

1. $\int_0^2 x(x^2-1)^3 dx$

let $u = (x^2-1)$ then $du = 2x dx$
so $x dx = \frac{1}{2} du$

if $x=0$ then $u=-1$

if $x=2$ then $u=2^2-1=3$

so substituting gives $\frac{1}{2} \int_{-1}^3 u^3 du = \frac{1}{2} \left(\frac{1}{4} u^4 \right) \Big|_{-1}^3$
 $= \frac{1}{8} u^4 \Big|_{-1}^3 = \frac{1}{8} \left(\frac{81}{16} \right) - \frac{1}{8} (1)$
 $= \frac{80}{8} = 10 \text{ sq. units}$

2. $\int_0^1 x^2(2x^3-1)^4 dx$

let $u = (2x^3-1)$ then $du = 6x^2 dx$

so $\frac{1}{6} du = x^2 dx$

if $x=0$ then $u=-1$ but if $x=1$ then $u=1$

substituting gives

$\frac{1}{6} \int_{-1}^1 u^4 du = \frac{1}{6} \left(\frac{1}{5} u^5 \right) \Big|_{-1}^1 = \frac{1}{30} (+1) - \frac{1}{30} (-1)$
 $= \frac{1}{30} + \frac{1}{30} = \frac{2}{30} = \frac{1}{15} \text{ sq. units}$

6.5 Pg 463 (cont. 9, 10, 15, 29)

$$9. \int_1^3 (2x-1)^4 dx$$

$$\text{let } u = (2x-1) \text{ Then } du = 2dx$$

$$\text{so } \frac{1}{2} du = dx$$

if $x=1$ Then $u = 2(1)-1 = 1$ and if $x=3$ Then $u = 5$

so substituting above gives

$$\frac{1}{2} \int_1^5 u^4 du = \frac{1}{2} \left(\frac{1}{5} \right) u^5 \Big|_1^5 = \frac{1}{10} (3125) - \frac{1}{10} (1) = \frac{3124}{10}$$

$$= 312.4 \text{ sq. units}$$

$$10. \int_1^2 (2x+4)(x^2+4x-8)^3 dx$$

$$\text{let } u = (x^2+4x-8) \text{ Then } du = (2x+4) dx$$

if $x=1$ Then $u = -3$ and if $x=2$ Then $u = 4$

substituting from above gives

$$\int_{-3}^4 u^3 du = \left(\frac{1}{4} \right) u^4 \Big|_{-3}^4 = \left(\frac{1}{4} \right) (64) - \left(\frac{1}{4} \right) (81)$$

$$= 64 - \frac{81}{4} = 64 - 20\frac{1}{4}$$

$$= 43\frac{3}{4} \text{ sq. units}$$

6.5 Pg 463 (15, 29) cont.

$$15. \int_0^2 2x e^{x^2} dx$$

~~let $u = e^{x^2}$ then $du = (2x)(e^{x^2}) dx$~~ Too much \downarrow

Try again

let $u = x^2$ then $du = 2x dx$

if $x=0$ then $u=0$ and if $x=2$ then $u=4$

substituting above info gives

$$\int_0^4 e^u du = (1) e^u \Big|_0^4 = e^4 - e^0 = e^4 - 1$$

sq. units

29. Find the area of the region under the graph of f on $[a, b]$; $f(x) = x^2 - 2x + 2$; $[-1, 2]$

$$\int_{-1}^2 (x^2 - 2x + 2) dx$$

$$= \frac{1}{3} x^3 - 2\left(\frac{1}{2}\right) x^2 + 2x \Big|_{-1}^2$$

$$= \left(\frac{1}{3}(8) - 2^2 + 2(2)\right) - \left(\frac{1}{3}(-1)^3 - (-1) + 2(-1)\right)$$

$$= \left(\frac{8}{3} - 4 + 4\right) - \left(-\frac{1}{3} - 1 - 2\right)$$

$$= \frac{8}{3} - \left(-\frac{10}{3}\right) = \frac{8}{3} + \frac{10}{3} = \frac{18}{3} = 6$$

sq. units