

3.2 Exercises

In Exercises 1–30, find the derivative of each function.

1. $f(x) = 2x(x^2 + 1)$

2. $f(x) = 3x^2(x - 1)$

3. $f(t) = (t - 1)(2t + 1)$

4. $f(x) = (2x + 3)(3x - 4)$

5. $f(x) = (3x + 1)(x^2 - 2)$

6. $f(x) = (x + 1)(2x^2 - 3x + 1)$

7. $f(x) = (x^3 - 1)(x + 1)$

8. $f(x) = (x^3 - 12x)(3x^2 + 2x)$

9. $f(w) = (w^3 - w^2 + w - 1)(w^2 + 2)$

10. $f(x) = \frac{1}{5}x^5 + (x^2 + 1)(x^2 - x - 1) + 28$

11. $f(x) = (5x^2 + 1)(2\sqrt{x} - 1)$

12. $f(t) = (1 + \sqrt{t})(2t^2 - 3)$

13. $f(x) = (x^2 - 5x + 2)\left(x - \frac{2}{x}\right)$

14. $f(x) = (x^3 + 2x + 1)\left(2 + \frac{1}{x^2}\right)$

15. $f(x) = \frac{1}{x - 2}$

16. $g(x) = \frac{3}{2x + 4} + 2x^2$

17. $f(x) = \frac{2x - 1}{2x + 1}$

18. $f(t) = \frac{1 - 2t}{1 + 3t}$

19. $f(x) = \frac{1}{x^2 + x + 2}$

20. $f(u) = \frac{u}{u^2 + 1}$

21. $f(s) = \frac{s^2 - 4}{s + 1}$

22. $f(x) = \frac{x^3 - 2}{x^2 + 1}$

23. $f(x) = \frac{\sqrt{x} + 1}{x^2 + 1}$

24. $f(x) = \frac{x}{\sqrt{x} + 2}$

25. $f(x) = \frac{x^2 + 2}{x^2 + x + 1}$

26. $f(x) = \frac{x + 1}{2x^2 + 2x + 3}$

27. $f(x) = \frac{(x + 1)(x^2 + 1)}{x - 2}$

28. $f(x) = (3x^2 - 1)\left(x^2 - \frac{1}{x}\right)$

29. $f(x) = \frac{x}{x^2 - 4} - \frac{x - 1}{x^2 + 4}$

30. $f(x) = \frac{x + \sqrt{3x}}{3x - 1}$

In Exercises 31–34, suppose f and g are functions that are differentiable at $x = 1$ and that $f(1) = 2$, $f'(1) = -1$, $g(1) = -2$, and $g'(1) = 3$. Find the value of $h'(1)$.

31. $h(x) = f(x)g(x)$

32. $h(x) = (x^2 + 1)g(x)$

33. $h(x) = \frac{xf(x)}{x + g(x)}$

34. $h(x) = \frac{f(x)g(x)}{f(x) - g(x)}$